### CSE4203: Computer Graphics Chapter – 7 (part - A) **Viewing**

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# Outline

- Image-order and object-render rendering
- Viewing transformation
- Viewport transformation
- Orthographic projection transformation

## Credit

#### Fundamentals of Computer Graphics

<complex-block>

#### CS4620: Introduction to Computer Graphics

Cornell University Instructor: Steve Marschner <u>http://www.cs.cornell.edu/courses/cs46</u> 20/2019fa/

# Rendering Techniques (1/2)

- One of the basic tasks of computer graphics is rendering 3D objects:
  - taking a scene, or model, composed of many geometric objects arranged in 3D space
  - producing a 2D image that shows the objects as viewed
  - from a particular viewpoint.

# Rendering Techniques (2/2)

- 1. <u>Image-order rendering</u>: iterate over the pixels in the image to be produced, rather than the elements in the scene to be rendered.
- 2. <u>object-order rendering:</u> that iterate over the elements in the scene to be rendered, rather than the pixels in the image to be produced.

## Image-order Rendering (1/2)

- Image-order rendering:
  - Ray-tracing:

Each pixel is considered in turn, and for each pixel

- All the objects that influence it are found
- and the pixel value is computed.
  - in Chapter 4

## Object-order Rendering (1/2)

- Object-order rendering:
  - Viewing Transformation:

Each object is considered in turn, and for each object:

• All the pixels that it influences are found and updated

Credit: Fundamentals of Computer Graphics 3rd Edition by Peter Shirley, Steve Marschner | http://www.cs.cornell.edu/courses/cs4620/2019fa/

# Object-order Rendering (2/2)

- Viewing Transformation (this chapter):
  - The inverse of the previous process.
  - How to use *matrix transformations* to express any parallel or perspective view.
  - These transformations:
    - Project 3D points in the scene (world space) to 2D points in the image (image space)

## Object space vs World space vs Camera space

Object space

- World space

– Camera space

#### Viewing Transformation Sequences (1/1)



Credit: Fundamentals of Computer Graphics 3<sup>rd</sup> Edition by Peter Shirley, Steve Marschner | http://www.cs.cornell.edu/courses/cs4620/2019fa/

## Viewport Transformation (1/19)



• Projection: Ignoring the *z*-coordinate

## Viewport Transformation (2/19)

- Canonical View Volume:  $(x,y,z) \in [-1, 1]^3$ 
  - We will assume that the model to be drawn are completely inside the canonical view vol.



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## Viewport Transformation (4/19)



Credit: Fundamentals of Computer Graphics 3<sup>rd</sup> Edition by Peter Shirley, Steve Marschner | http://www.cs.cornell.edu/courses/cs4620/2019fa/

## Viewport Transformation (5/19)





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 $T(1, 1) \rightarrow S(nx/2, ny/2)$ 



 $T(1, 1) \rightarrow S(nx/2, ny/2) \rightarrow T(-1/2, -1/2)$ 



#### $T(1, 1) \rightarrow S(nx/2, ny/2) \rightarrow T(-1/2, -1/2)$ $M_{vp} = T(-1/2, -1/2) * S(nx/2, ny/2) * T(1,1)$

## Viewport Transformation (15/19)

 $M_{vp} = T(-1/2, -1/2) * S(nx/2, ny/2) * T(1, 1)$ 

$$\begin{bmatrix} \frac{n_x}{2} & 0 & \frac{n_x-1}{2} \\ 0 & \frac{n_y}{2} & \frac{n_y-1}{2} \\ 0 & 0 & 1 \end{bmatrix}$$
Q: Do matrix  
multiplication and check

## Viewport Transformation (16/19)

 $M_{vp} = T(-1/2, -1/2) * S(nx/2, ny/2) * T(1, 1)$ 



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## Viewport Transformation (18/19)



$$M_{\rm vp} = \begin{bmatrix} \frac{n_x}{2} & 0 & 0 & \frac{n_x - 1}{2} \\ 0 & \frac{n_y}{2} & 0 & \frac{n_y - 1}{2} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

## Viewport Transformation (19/19)



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## Orthographic Projection Transformation (1/1)

• What if we want to render geometry in some region other than canonical view vol.?



# Orthographic View Volume (1/3)

- We'll name the coordinates of its sides so that the view volume is [I, r] × [b, t] × [f, n]
  - View direction: *looking along -z*
  - Orientation: +y up
    - $x = l \equiv left plane$ ,
    - $x = r \equiv right plane$ ,
    - $y = b \equiv bottom plane$ ,
    - $y = t \equiv top plane$ ,
    - $z = n \equiv near plane$ ,
    - $z = f \equiv far plane$ .



# Orthographic View Volume (2/3)

- Looking along the *minus z-axis* with his head pointing in the *positive y-direction*.
  - View direction: *looking along –z*
  - Orientation: +y up
- But, this is unintuitive!



## Orthographic View Volume (3/3)

- If entire orthographic view volume has negative z then n > f.
  - *z* = *n* plane is closer



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# Orthographic to Canonical View Volume (1/3)

- Transform from orthographic view volume to the canonical view volume
  - We need to apply *windowing transformation* (just like before!)



Credit: Fundamentals of Computer Graphics 3rd Edition by Peter Shirley, Steve Marschner | http://www.cs.cornell.edu/courses/cs4620/2019fa/

## Orthographic to Canonical View Volume (2/3)

$$\mathbf{M}_{\text{orth}} = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{2}{n-f} & -\frac{n+f}{n-f} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



## Orthographic to Canonical View Volume (3/3)

$$\mathbf{M}_{\text{orth}} = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{2}{n-f} & -\frac{n+f}{n-f} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{array}{l} \text{Q: How can we get this} \\ \text{matrix?} \\ \text{Help: Chap 6 (Windowing} \\ \text{Transformation) and } M_{vp} \end{array}$$



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#### Orthographic $\rightarrow$ Canonical $\rightarrow$ Screen (1/5)



 $\geq$ 

#### Orthographic $\rightarrow$ Canonical $\rightarrow$ Screen (2/5)



#### Orthographic $\rightarrow$ Canonical $\rightarrow$ Screen (3/5)



#### Orthographic $\rightarrow$ Canonical $\rightarrow$ Screen (4/5)



#### Orthographic $\rightarrow$ Canonical $\rightarrow$ Screen (5/5)



#### Code: Orthographic to Screen (1/1)

#### Drawing many 3D lines with endpoints $a_i$ and $b_i$ :

```
Construct M_{vp}
Construct M_{orth}
M = M_{vp} * M_{orth}
for each line segment (a_i, b_i) do:
p = M * a_i
q = M * b_i
drawline (x_p, y_p, x_q, y_q)
```

## Practice Problem - 1

Transform a 3D line AB from an *orthographic view volume* to a *viewport* of size 128 x 96. Vertices of the line are A(-1, -3, -5) and B(2, 4, -6). The orthographic view volume has the following setup:

You must -

- a. Determine the transformation matrix *M*.
- b. Multiply *M* with the vertices of the line and determine the position of vertices on viewport.

### Practice Problem – 1 (Sol.)

$$M_{\rm vp} = \begin{bmatrix} \frac{n_x}{2} & 0 & 0 & \frac{n_x - 1}{2} \\ 0 & \frac{n_y}{2} & 0 & \frac{n_y - 1}{2} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 nx = 128  
ny = 96

$$\mathbf{M}_{\text{orth}} = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{2}{n-f} & -\frac{n+f}{n-f} \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \begin{bmatrix} \mathsf{I} = -4, \mathsf{r} = 4, \\ \mathsf{b} = -4, \mathsf{t} = 4, \\ \mathsf{n} = -4, \mathsf{f} = -8 \end{bmatrix}$$

### Practice Problem – 1 (Sol.)

 $M = M_{vp}^* M_{orth}$ 

$$\mathbf{M} = \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & -\frac{r+l}{r-l} \\ 0 & \frac{2}{t-b} & 0 & -\frac{t+b}{t-b} \\ 0 & 0 & \frac{2}{n-f} & -\frac{n+f}{n-f} \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{n_x}{2} & 0 & 0 & \frac{n_x-1}{2} \\ 0 & \frac{n_y}{2} & 0 & \frac{n_y-1}{2} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

A' = M A

B' = M B

## **Additional Reading**

- Wireframe renderings
- Derive M<sub>orth</sub>